(1) Prove that the order of any group element is equal to the order of its inverse.

(2) Prove that the order of  $a^5$  is less than or equal to the order of a for any element a of any finite group.

(3) Give an example of a group and an element a for which  $1 < o(a^2) < o(a)$ .