

MATH 19-01: MATHEMATICS OF SOCIAL CHOICE

TUFTS UNIVERSITY DEPARTMENT OF MATHEMATICS
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- (1) Explain: if a 3-candidate election has two Smith candidates out of three, then there must be a tie in the pairwise comparison graph.
- (2) Find a preference schedule and system for which there is a spoiler who is a Smith candidate. In your example, are they a winning spoiler? Losing spoiler? Weak spoiler?
- (3) If there are $n = 10$ candidates, how many consolidations do you have to consider to run each of these methods?: plurality, runoff, elimination, Coombs, Borda, Smith, Smithified plurality, pairwise comparison, sequential, and dictatorship.
- (4) What has to be true about a pairwise comparison graph for it to be helpful in checking whether a system is unanimity-fair? Supposing $N = 100$ voters and $n = 5$ candidates, draw an example of a PWCG with one unanimous preference, and explain what you would have to check about \mathcal{W} if considering unanimity-fairness of your system.
- (5) Build a preference schedule with a Condorcet candidate and a cycle.
- (6) Build a preference schedule where nobody has 40% of the first-place votes, but there is some consolidation which produces a majority candidate.
- (7) Explain: the runoff method is unanimity-fair.